

# Generic Modelling of Energy Management Methods in Hybrid Energy Systems Including Energy Storage

Damian Giaouris

Senior Lecturer in Control of Electrical Systems

Newcastle University

Damian.Giaouris@ncl.ac.uk

Damian Giaouris<sup>a</sup>, Athanasios I. Papadopoulos<sup>b</sup>, Chrysovalantou Ziogou<sup>b</sup>, Spyros Voutetakis<sup>b</sup>,  
Simira Papadopoulou<sup>b</sup>, Panos Seferlis<sup>c</sup>, Charalampos Patsios<sup>a</sup>, Phil Taylor<sup>a</sup>

<sup>a</sup>Newcastle University, School of Electrical & Electronic Engineering, Newcastle Upon Tyne, UK

<sup>b</sup>Chemical Process and Energy Resources Institute, Centre for Research and Technology Hellas,  
Thermi-Thessaloniki, Greece

<sup>c</sup>Department of Mechanical Engineering, Aristotle University of Thessaloniki, Greece

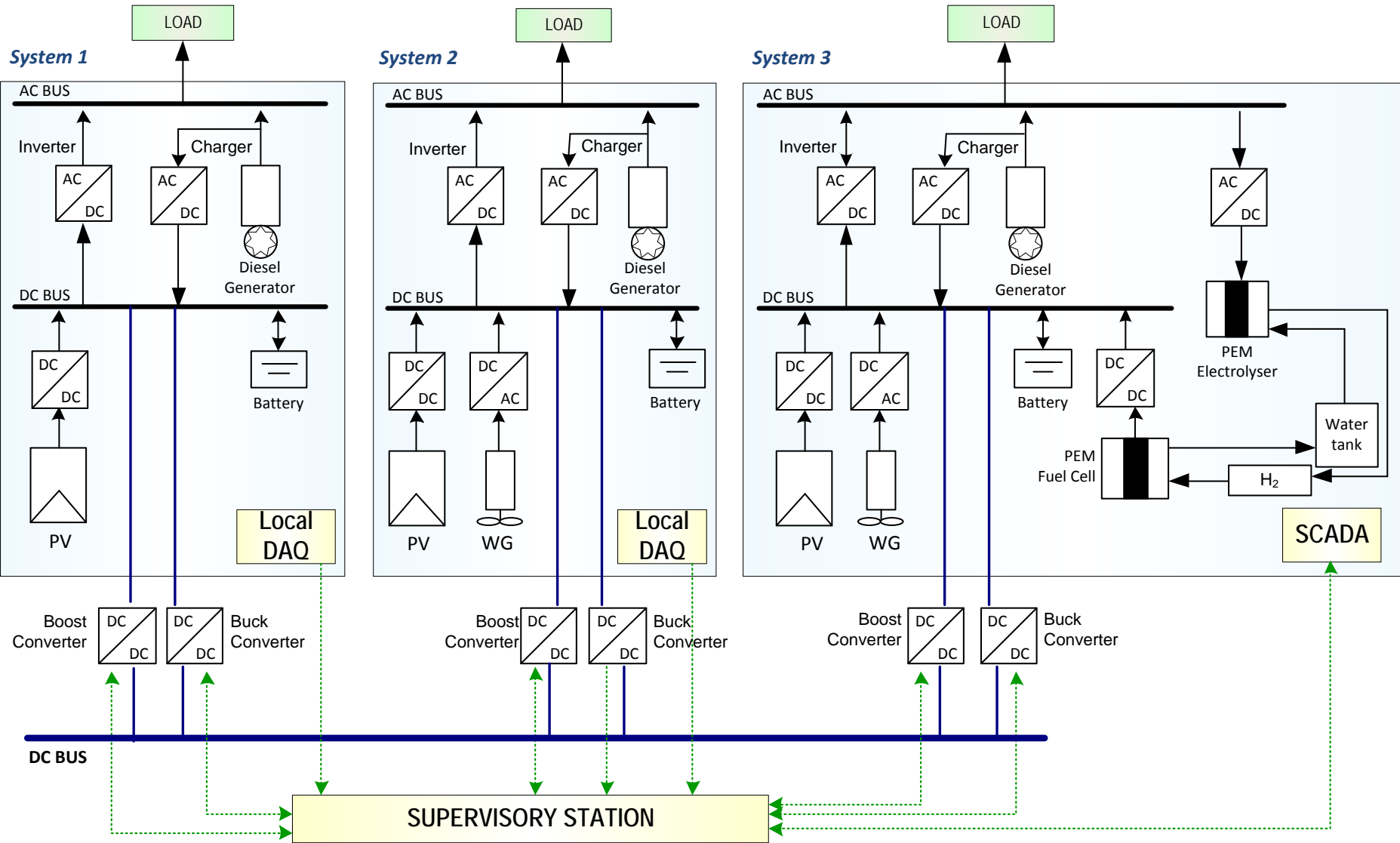


# Outline

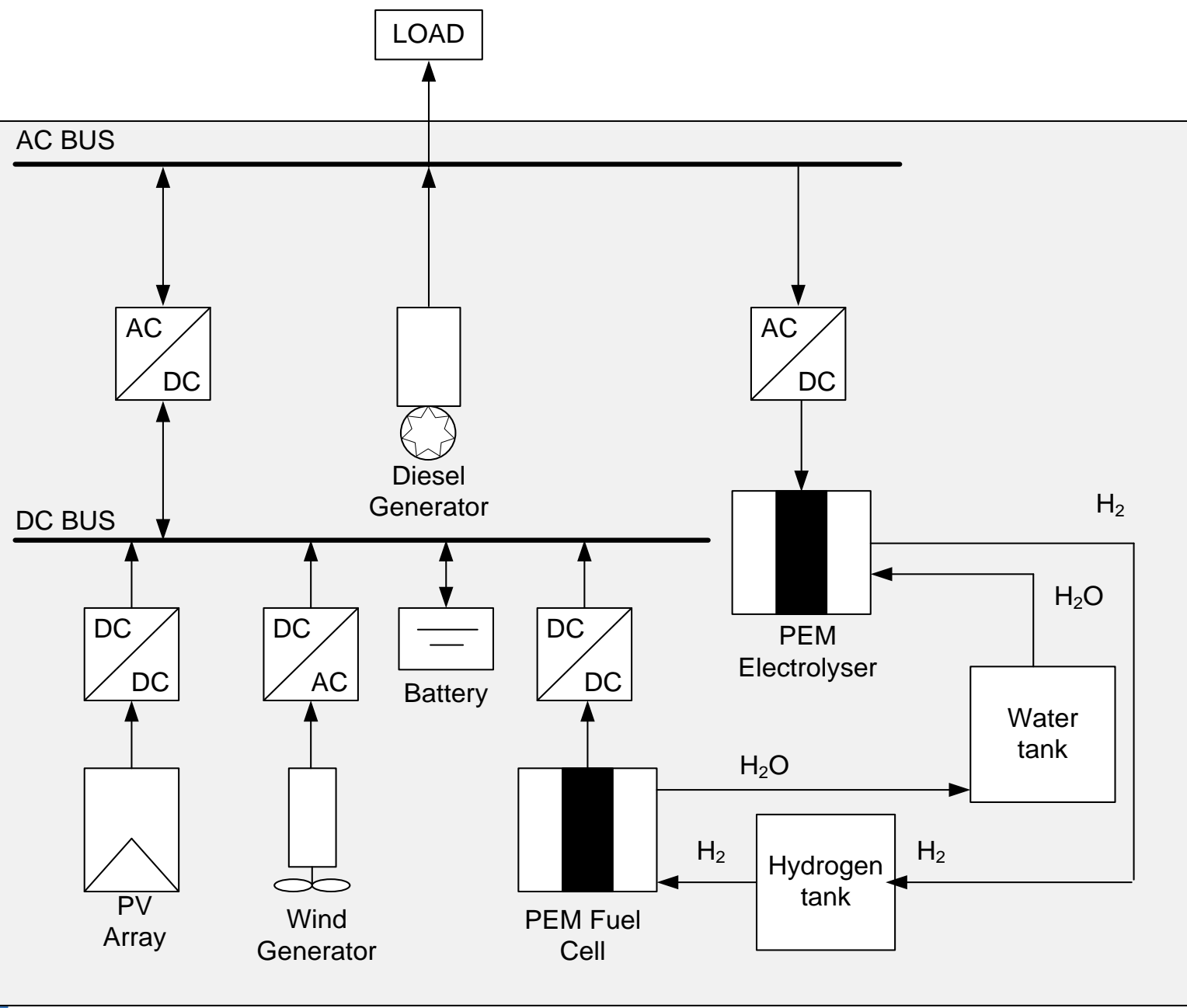
- **Energy Management Methods & Flow Charts**
- **State of (Directed) Graph**
- **Evolution Operator**
- **Complete Modelling**
- **Case Studies**



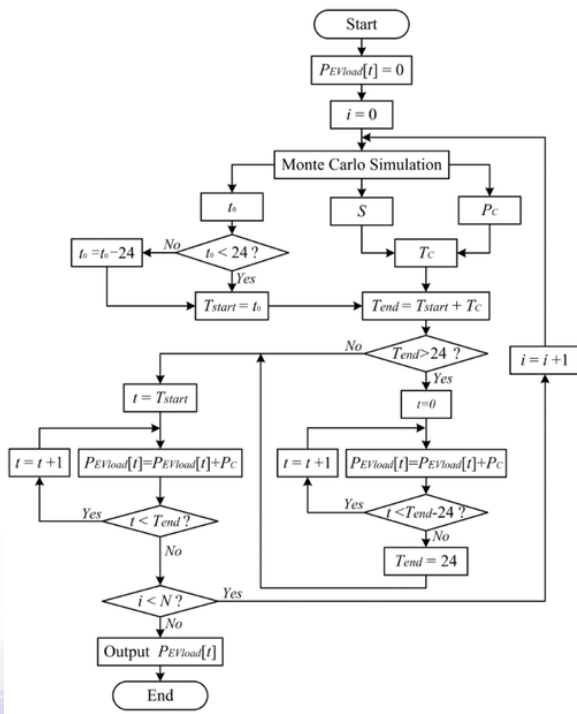
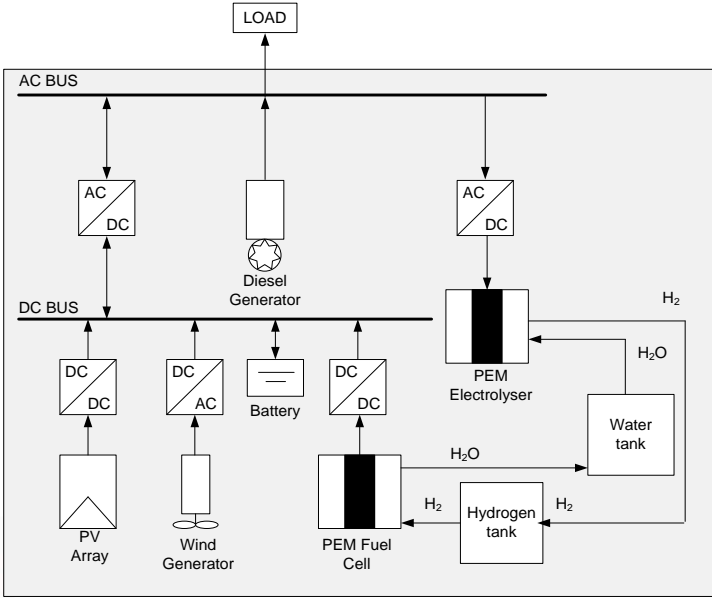
# Motivating example...



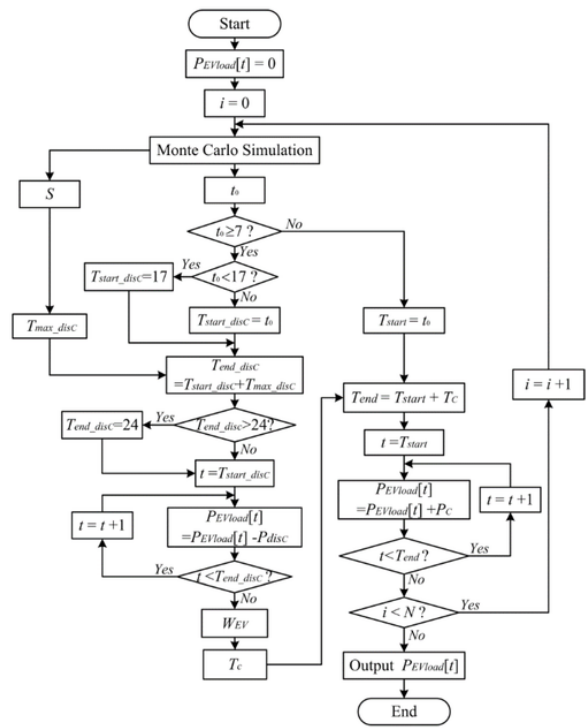
# Hybrid Energy System



# Energy Management Methods (EMM)



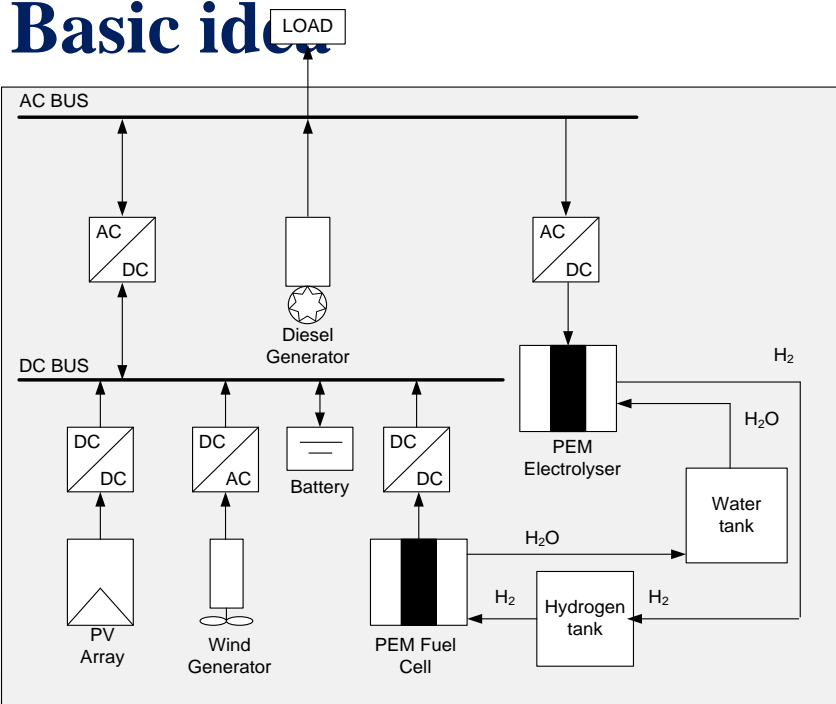
(a)



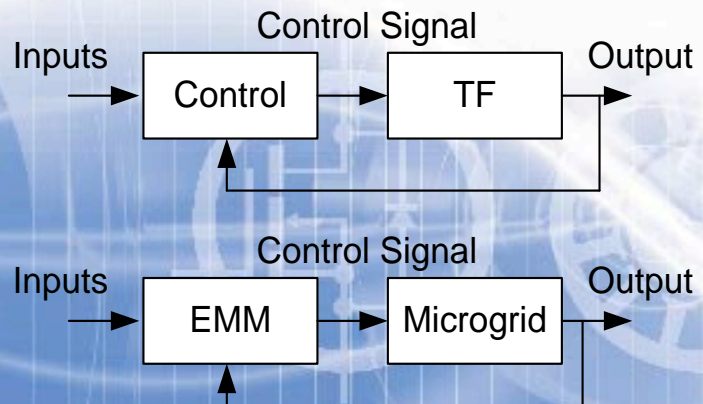
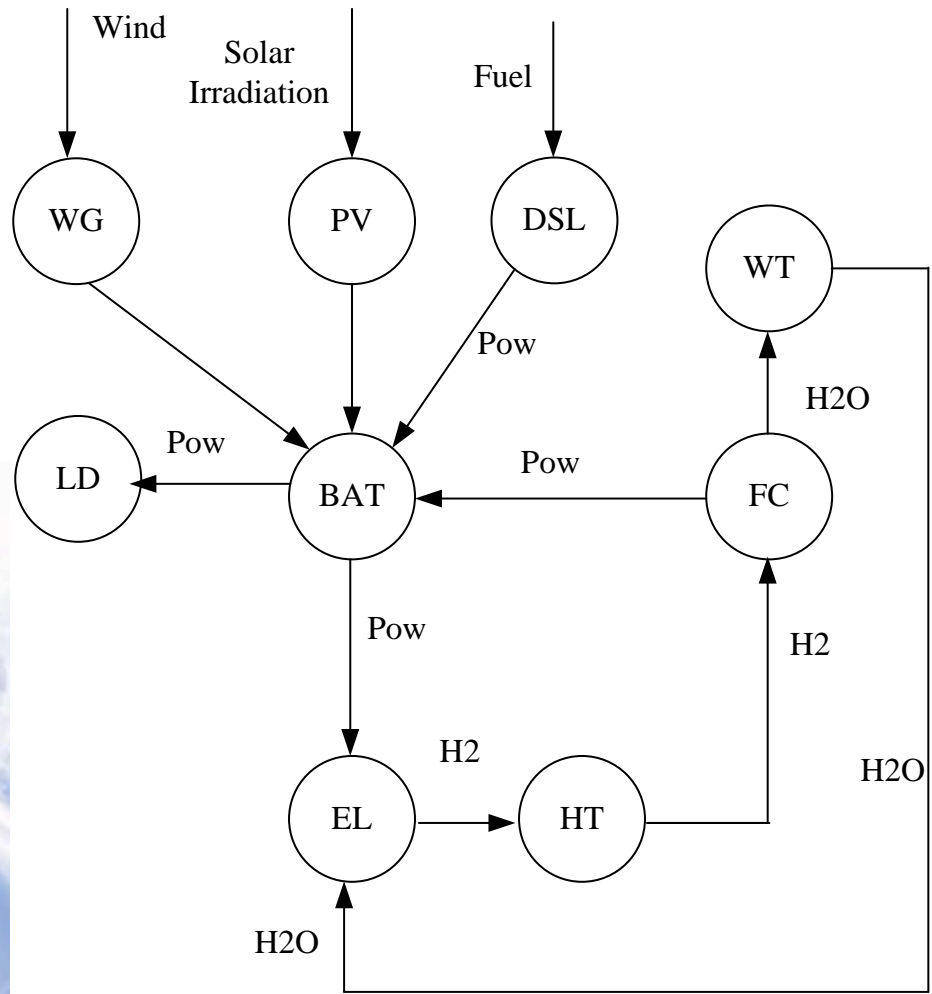
(b)



# Basic idea



- Try to define/describe an EMM/microgrid by stating their main properties
- Control theory: mathematical models (ODEs, TFs, state space models...)

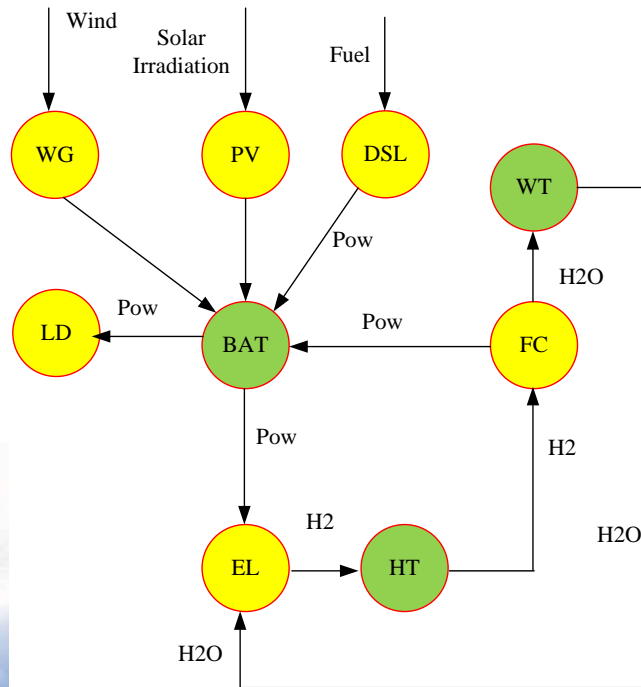


**Dynamical System<sup>1</sup>:**  
**{time, state of system, evolution operator}**

<sup>1</sup> Elements of Applied Bifurcation Theory, Yuri Kuznetsov, Springer-Verlag New York, Chapter 1.



# State of Graph



- Edges  $F_{m \rightarrow n}^j(t)$   $F_{FC \rightarrow BAT}^{POW}(t)$   $F_{EL \rightarrow HT}^{H_2}(t)$

- Nodes

- Accumulators  $SOAcc^l(t) \in [0,1], l \in \{BAT, HT, WT\}$

- Converters  $\varepsilon_i(t) \in \{0,1\}, i \in \{FC, EL, PV \dots\}$

State of graph =  $\{F_{m \rightarrow n}^j(t), SOAcc^l(t), \varepsilon_i(t)\}$

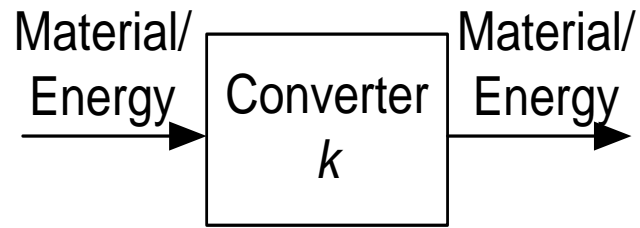
# Evolution Operator

EMM = How to operate these converters

EMM = Evolution operator =  $\varepsilon_i(t)$



# Converter Operation



$$\varepsilon_k(t) = f(x(t), u(t), P(t))$$

$$x(t) = \{F_{m \rightarrow n}^j(t), SOAcc^l(t), \varepsilon_i(t)\}$$

$$u(t) = [\text{Solar Irradiation, load profile...}]$$

$$P(t) = [\text{constraints, demanded values...}]$$

Required  $\varepsilon_k^{\text{Req}}(t)$

Availability  $\varepsilon_k^{\text{Avl}}(t)$

General Condition  $\varepsilon_k^{\text{Gen}}(t)$

$$\varepsilon_k(t) = L\{\varepsilon_k^{\text{Avl}}(t), \varepsilon_k^{\text{Req}}(t), \varepsilon_k^{\text{Gen}}(t)\}^2$$





# Example

“The state of charge of the battery is low”

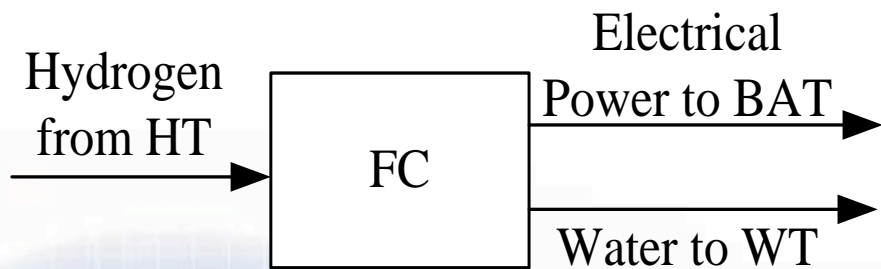
“There is available H<sub>2</sub> in the Hydrogen Tank”

“The Water Tank is not completely full”

$$\rho_{FC}^{SOAcc^{BAT}}(t) = SOAcc^{BAT}(t) < Lo_{FC}^{SOAcc^{BAT}}(t)$$

$$\rho_{FC}^{SOAcc^{HT}}(t) = SOAcc^{HT}(t) > Lo_{FC}^{SOAcc^{HT}}(t)$$

$$\rho_{FC}^{SOAcc^{WT}}(t) = SOAcc^{WT}(t) < Up_{FC}^{SOAcc^{WT}}(t)$$

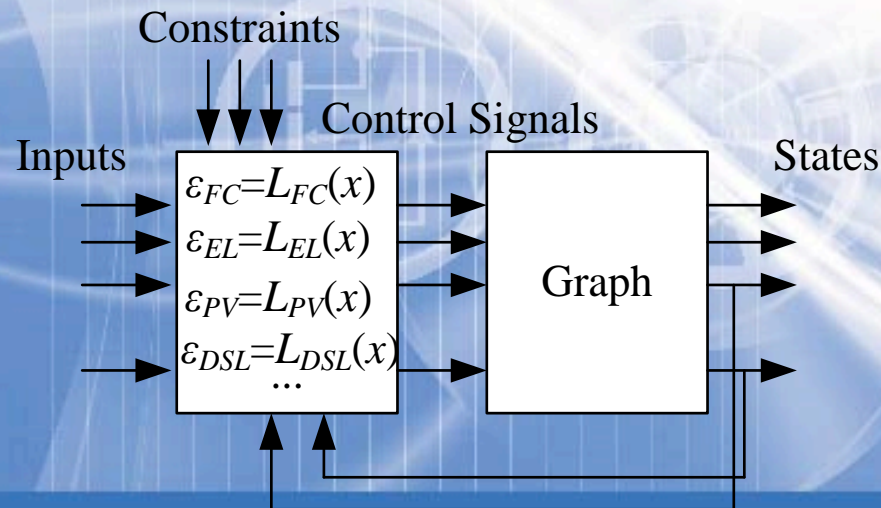


$$\varepsilon_{FC}^{Avl}(t) = \rho_{FC}^{SOAcc^{HT}}(t) \wedge \rho_{FC}^{SOAcc^{WT}}(t)$$

$$\varepsilon_{FC}^{Req}(t) = \rho_{FC}^{SOAcc^{BAT}}(t)$$

$$\varepsilon_{FC}^{Gen}(t) = [\varepsilon_{DSL}(t^-) = 0]$$

$$\varepsilon_{FC}(t) = \varepsilon_{FC}^{Avl}(t) \wedge \varepsilon_{FC}^{Req}(t) \wedge \varepsilon_{FC}^{Gen}(t)$$





# FC and EL

$$\rho_{EL \rightarrow HT}^{SOAcc^{BAT}}(t) = SOAcc^{BAT}(t) > str_{EL \rightarrow BF}^{SOAcc^{BAT}}(t)$$

$$\rho_{EL \rightarrow HT}^{SOAcc^{WT}}(t) = SOAcc^{WT}(t) > str_{EL \rightarrow HT}^{SOAcc^{WT}}(t)$$

$$\rho_{EL \rightarrow HT}^{SOAcc^{BF}}(t) = SOAcc^{BF}(t) < str_{EL \rightarrow HT}^{SOAcc^{BF}}(t)$$

$$\varepsilon_{EL}(t) = \rho_{EL \rightarrow HT}^{SOAcc^{BAT}}(t) \wedge \rho_{EL \rightarrow HT}^{SOAcc^{WT}}(t) \wedge \rho_{EL \rightarrow HT}^{SOAcc^{BF}}(t)$$

$$\rho_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) = SOAcc^{BAT}(t) < str_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t)$$

$$\rho_{FC \rightarrow BAT}^{SOAcc^{FT}}(t) = SOAcc^{FT}(t) > str_{FC \rightarrow BAT}^{SOAcc^{FT}}(t)$$

$$\rho_{FC \rightarrow BAT}^{SOAcc^{WT}}(t) = SOAcc^{WT}(t) < str_{FC \rightarrow BAT}^{SOAcc^{WT}}(t)$$

$$\varepsilon_{FC}(t) = \rho_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) \wedge \rho_{FC \rightarrow BAT}^{SOAcc^{FT}}(t) \wedge \rho_{FC \rightarrow BAT}^{SOAcc^{WT}}(t)$$



# Ignore specific conditions

$$\rho_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) = SOAcc^{BAT}(t) < str_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t)$$

$$\rho_{FC \rightarrow BAT}^{SOAcc^{FT}}(t) = SOAcc^{FT}(t) > str_{FC \rightarrow BAT}^{SOAcc^{FT}}(t)$$

$$\rho_{FC \rightarrow BAT}^{SOAcc^{WT}}(t) = SOAcc^{WT}(t) < str_{FC \rightarrow BAT}^{SOAcc^{WT}}(t)$$

$$\varepsilon_{FC}(t) = \rho_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) \wedge \rho_{FC \rightarrow BAT}^{SOAcc^{FT}}(t) \wedge \rho_{FC \rightarrow BAT}^{SOAcc^{WT}}(t)$$

$$\varepsilon_{FC}(t) = \left[ \rho_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) \wedge r_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) \right] \vee \left[ \left[ r_{FC \rightarrow BAT}^{SOAcc^{FT}}(t) \vee \rho_{FC \rightarrow BAT}^{SOAcc^{FT}}(t) \right] \wedge \left[ r_{FC \rightarrow BAT}^{SOAcc^{WT}}(t) \vee \rho_{FC \rightarrow BAT}^{SOAcc^{WT}}(t) \right] \right]$$



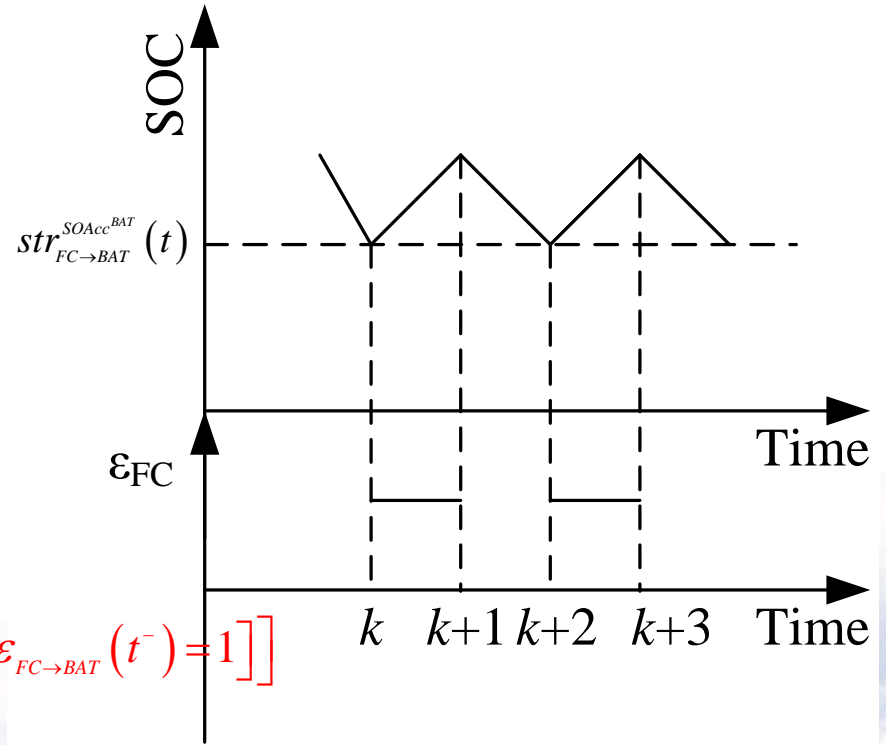
# Hysteresis zones for chattering

$$\rho_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) = SOAcc^{BAT}(t) < str_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t)$$

$$\rho_{FC \rightarrow BAT}^{SOAcc^{FT}}(t) = SOAcc^{FT}(t) > str_{FC \rightarrow BAT}^{SOAcc^{FT}}(t)$$

$$\rho_{FC \rightarrow BAT}^{SOAcc^{WT}}(t) = SOAcc^{WT}(t) < str_{FC \rightarrow BAT}^{SOAcc^{WT}}(t)$$

$$\varepsilon_{FC}(t) = \rho_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) \wedge \rho_{FC \rightarrow BAT}^{SOAcc^{FT}}(t) \wedge \rho_{FC \rightarrow BAT}^{SOAcc^{WT}}(t)$$



$$\rho_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) = [SOAcc^{BAT}(t) < str_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t)]$$

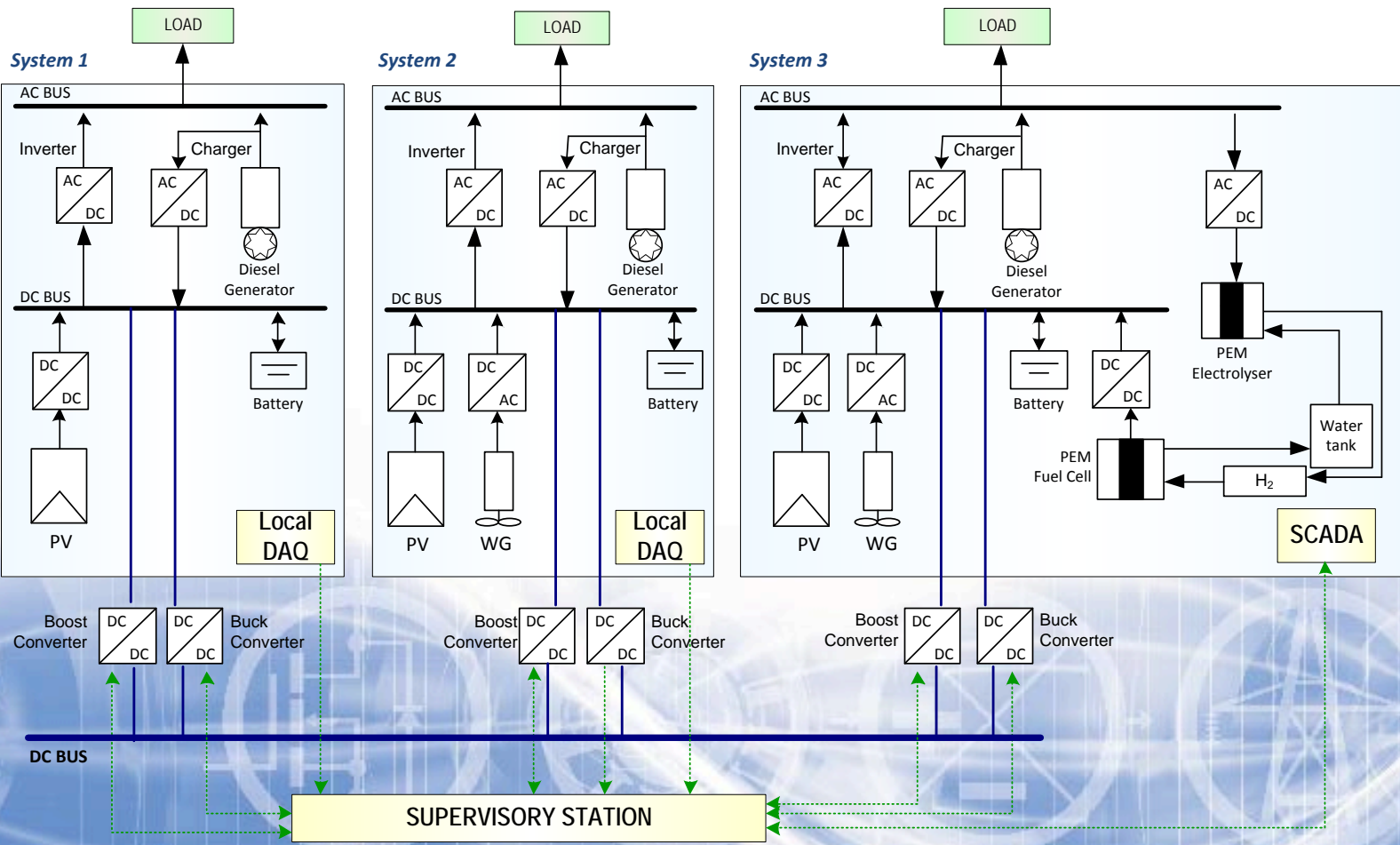
$$\vee [[str_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) < SOAcc^{BAT}(t) < stp_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t)] \wedge [\varepsilon_{FC \rightarrow BAT}(t^-) = 1]]$$

# Compact expression

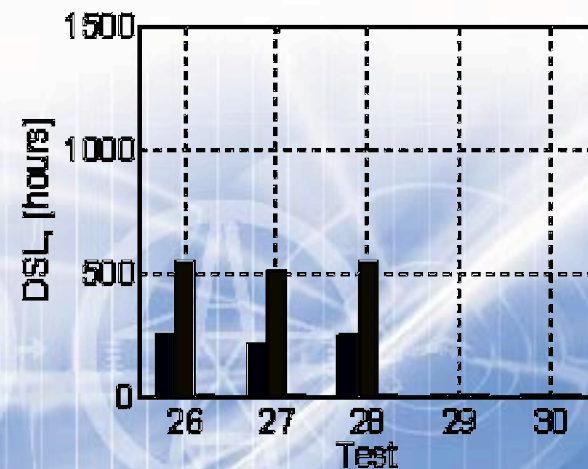
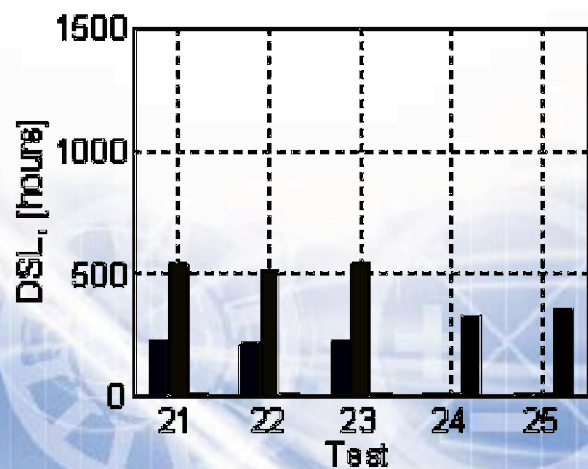
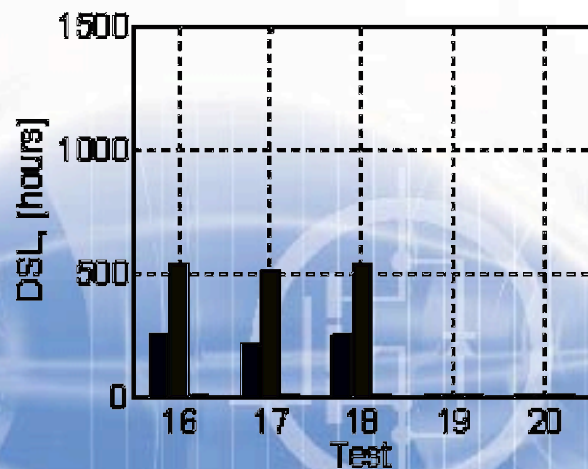
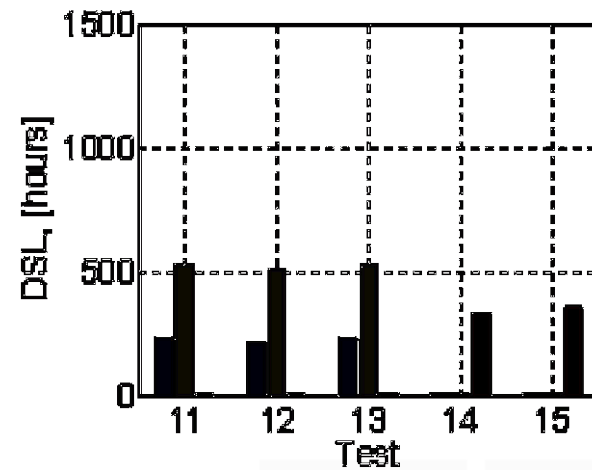
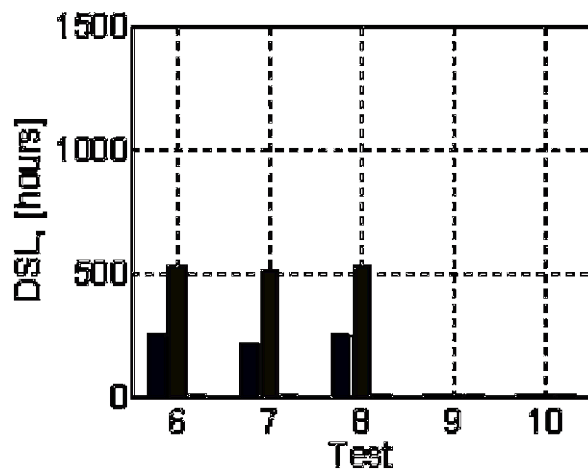
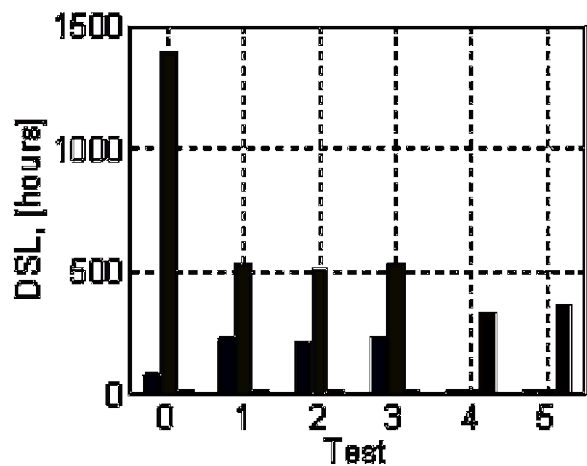
$$\begin{aligned}
 \mathcal{E}_{FC \rightarrow BAT}(t) & \quad \bigcap_c \left[ \mathcal{E}_{FC \rightarrow BAT}^c(t) \right], c \in \{Avl, Req, Gen\} \\
 \mathcal{E}_{FC \rightarrow BAT}^{Avl}(t) & \quad \bigcap_l \left[ r_{FC \rightarrow BAT}^{SOAcc^l}(t) \vee \rho_{FC \rightarrow BAT}^{SOAcc^l}(t) \right], l \in \{FT, WT\} \\
 \mathcal{E}_{FC \rightarrow BAT}^{Gen}(t) & \quad 1 \\
 \mathcal{E}_{FC \rightarrow BAT}^{Req}(t) & \quad \rho_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) \vee r_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) \\
 \rho_{FC \rightarrow BAT}^{SOAcc^{FT}}(t) & \quad SOAcc^{FT}(t) > str_{FC \rightarrow BAT}^{SOAcc^{FT}} \\
 \rho_{FC \rightarrow BAT}^{SOAcc^{WT}}(t) & \quad SOAcc^{WT}(t) < str_{FC \rightarrow BAT}^{SOAcc^{WT}} \\
 & \quad \left[ SOAcc^{BAT}(t) < str_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) \right] \vee \\
 \rho_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) & \quad \left[ \left[ str_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) < SOAcc^{BAT}(t) < stp_{FC \rightarrow BAT}^{SOAcc^{BAT}}(t) \right] \right] \\
 & \quad \wedge \left[ \mathcal{E}_{FC \rightarrow BAT}(t^-) \right]
 \end{aligned}$$



# Results



# Results<sup>2</sup>



<sup>2</sup> Giaouris et al, Performance investigation of a hybrid renewable power generation and storage system using systemic power management models, Energy, Vol. 61, pp. 621-635, Nov. 2013.





# Results...

$$\varepsilon_k(t) = f(x(t), u(t), P(t))$$

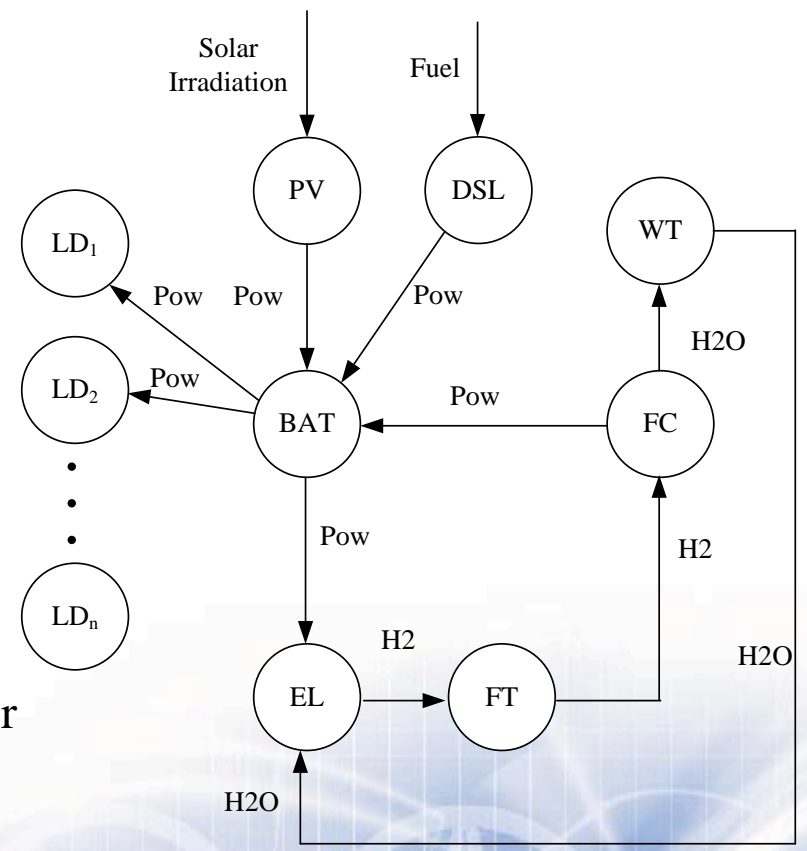
$$x(t) = \{F_{m \rightarrow n}^j(t), SOAcc^l(t), \varepsilon_i(t)\}$$

$$u(t) = [Solar\ Irradiation, load\ profile...]$$

$$P(t) = [constraints, demanded\ values...]$$

$$\varepsilon_{FC}(t) = (\varepsilon_{FC}^{Avl}(t) \wedge \varepsilon_{FC}^{Req}(t) \wedge \varepsilon_{FC}^{Gen}(t)) \vee \varepsilon_{FC}^{LD}(t)$$

Based on load/weather forecasting



# Results...

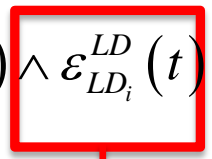
$$\varepsilon_k(t) = f(x(t), u(t), P(t))$$

$$x(t) = \{F_{m \rightarrow n}^j(t), SOAcc^l(t), \varepsilon_i(t)\}$$

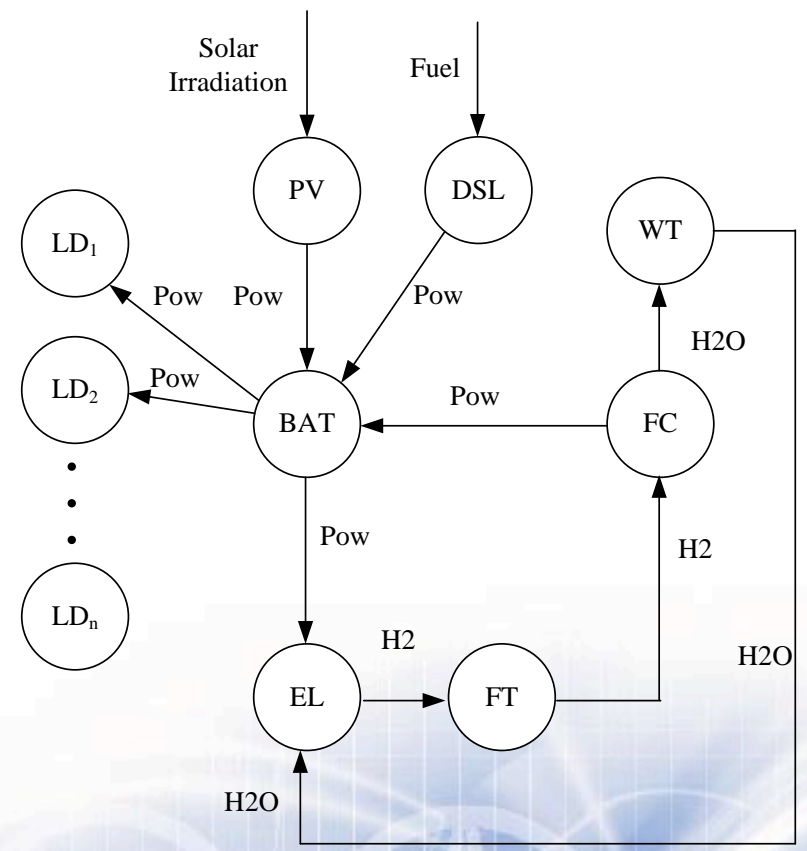
$$u(t) = [Solar\ Irradiation, load\ profile...]$$

$$P(t) = [constraints, demanded\ values...]$$

$$\varepsilon_{LD_i}(t) = \varepsilon_{LD_i}^{Avl}(t) \wedge \varepsilon_{LD_i}^{Req}(t) \wedge \varepsilon_{LD_i}^{Gen}(t) \wedge \varepsilon_{LD_i}^{LD}(t)$$



Load shifting



# Results...

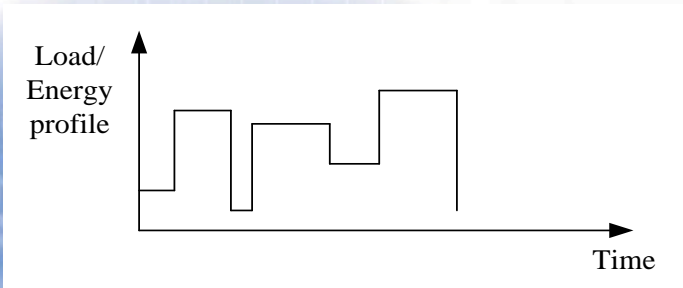
$$\varepsilon_k(t) = f(x(t), u(t), P(t))$$

$$x(t) = \{F_{m \rightarrow n}^j(t), SOAcc^l(t), \varepsilon_i(t)\}$$

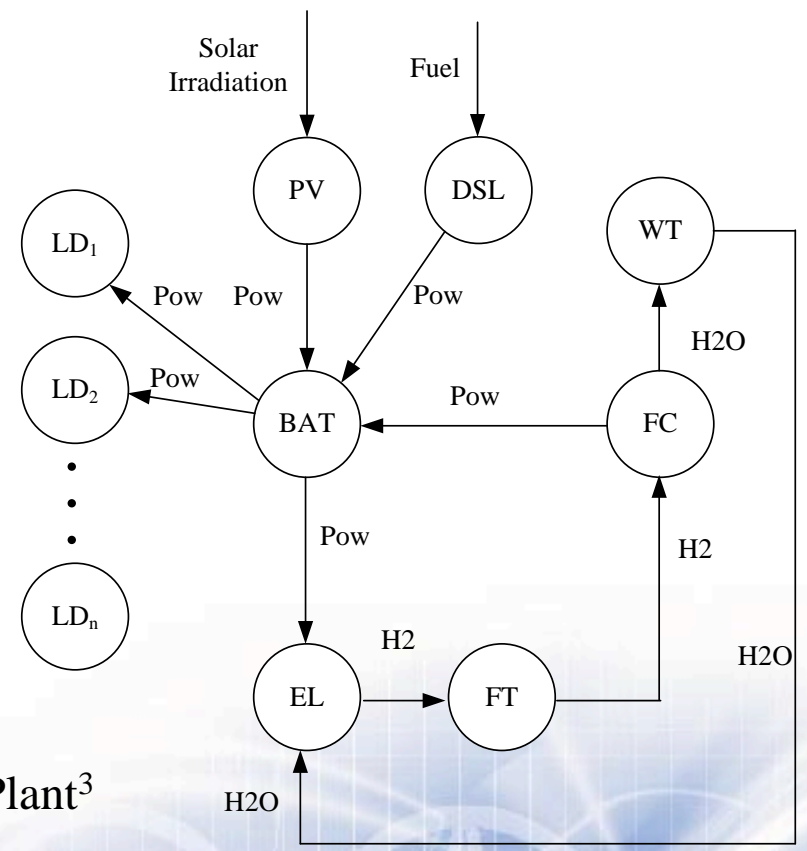
$$u(t) = [Solar\ Irradiation, load\ profile...]$$

$$P(t) = [constraints, demanded\ values...]$$

$$\rho_{FC}^{SOAcc^{BAT}}(t) = SOAcc^{BAT}(t) < Lo_{FC}^{SOAcc^{BAT}}(t)$$



Virtual Power Plant<sup>3</sup>



<sup>3</sup> Giaouris et al, Power grand composite curves shaping for adaptive energy management of hybrid microgrids, Renewable Energy, vol. 95, pp. 433-448, 2016.



# Summary

- A systematic approach to describe HES/EMM
  - Unified modelling approach
  - Study, Control, Optimise HES/EMM
- Several examples that include
  - Constant load
  - Multiple random loads
  - Load shifting
  - Generate specific load/energy profiles





**Newcastle  
University**



National Centre for  
Energy Systems  
Integration



School of Electrical and Electronic Engineering

# Any Questions?

